Quantlets, Quantnet, Applications

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Transparency and Reproducibility

- Required by good scientific practice
- Dormant/dead research materials/contributions
- Knowledge discovery



- Quantnet open access code-sharing platform
 - Quantlets: program codes (R, MATLAB, SAS), various authors
 - QuantNetXploRer



Example for a search query

Quantnet ::	$f(x \mid \mu, \sigma^{*}) = S\Phi(d_{1}) - Ke^{-iT}\Phi(d_{2})$ Start σ_{1}) - $\Pr(X_{n+1} - $	$\int_{\partial M} \exp\left(\frac{ \Phi - \mu^{2}}{2\pi}\right)$ $\int_{\partial M} \sum_{i=1}^{N} \frac{1}{P(A_{i} D)} = - \frac{1}{2} \frac{1}{P(A_{i} D)}$ $\int_{\partial M} \frac{1}{P(A_{i} D)} = - \frac{1}{2} \frac{1}{P(A_{i} D)}$
Start Info Imprint	ar(1)	Description
	Name	Platforms
	MVAnmdscar1	R 2.9.1
	MVAnmdscar1	MatLab R2007b
	SFEacfar1	📣 MatLab R2007b
	SFEacfar1	§ SAS 9.4

Figure 1: Search results for the search term "ar(1)" in the classical interface



Example for a search query



Figure 2: Search results for the search term "ar(1)" in the graphical interface

Quantnet Basics

1.11 1.11

1-3

Visualization



Figure 3: Quantlets from *SFE* (force directed scheme) and *MVA* (clustering scheme)

Quantnet Basics



1-4

Most frequent words/terms in QNet



Figure 4: Words with more then 90 occurrences



Motivation

Wordcloud of the words/terms in QNet

calcul model volatil varianc return histor the gumbel generation eigenvalu statist confid Valithern ordinari andwidth smar employ & Eform dis servers amenantur () align group and net ena gaussian zero sine stifty of rogener the portion of the portion o symession sampl 1 reflect black implement dsfmnumber "tree no option short smooth area of the linear boxplot probabl market miler affect from Index and the second se minimum provid likelihood forecast traffic index andrew related def ochast strike dataset to yaid novemb approxi dataset to yaid novemb approxi dataset to yaid novemb approxi to yaid novemb approxi to yaid novemb approxi transform signific amp renai inversivation generat process constraint dimension companimationan poisson har

1-6

Correlation graph of the QNet terms



Figure 5: 30 most frequent terms with treshold = 0.1



Correlation graph of the QNet terms



Figure 6: 30 most frequent terms with treshold = 0.05Quantnet Basics



Research Goals

Text Mining

- Model calibration
- Dimension reduction
- Semantic based Information Retrieval
- Document Clustering

Visualization

- Optimal projection into 2 dimensions
- Comparison of MDS, PCA and t-SNE
- Relationships between document similarity measures and 2D-Geometry



Outline

- 1. Motivation \checkmark
- 2. Interactive GUI
- 3. Vector Space Model (VSM)
- 4. Empirical results
- 5. Conclusion





 Searching parameters: Quantletname, Description, Datafile, Author

Data types: R, Matlab, SAS



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Integrated exploring and navigating

Projects



Keywords: Top 30

normal distribution option regression VaR returns PCA

call financial volatility cdf plot kernel DSFM portfolio pdf eigenvalues density visualization principal components random scatterplot time series simulation nonparametric CAT bond binomial Pareto boxplot interest rate

Click here for all Keywords...

Most Recent Quantlets

 $\label{eq:selectron} \begin{array}{l} {\rm SFENormalApprox1} \clubsuit, {\rm SFENormalApprox2} \Lambda, {\rm$



Interactive Structure



Figure 7: Quantlet MVAreturns containing the search term "time series"

Quantnet Basics

#clear variables and close windows setwd("C:/...") #Please change working directory ibm(-read.csv("ibm.csv") applec-read.csv("apple.csv") back-read.csv("bac.csv") fordc-read.csv("ford.csv") edk-read.csv("ed.csv") #compute the returns from assets a[i]<-(y1[i]-y1[i-1])/y1[i] b[i]<-(v2[i]-v2[i-1])/v2[i] d[i]<-(y3[i]-y3[i-1])/y3[i] Areturns for Bank of America Corporation f(i)<-(v4(i)-v4(i-1))/v4(i) g[i]<-(y5[i]-y5[i-1])/y5[i] Freturns for Consolidated Edison

Sec. \$

2-3



Figure 8: All Quantlets in QuantNetXploRer, search term "time series"



Vector Space Model (VSM)



- Model calibration
 - Text preprocessing
 - Text to Vector: Weighting scheme, Similarity, Distance
 - Basic VSM
 - Generalized VSM
 - LSA Latent Semantic Analysis



	terms	Non-/sparse entries
all terms (raw)	3229	26619/5162384
after preprocessing	2385	19936/3812759
discarding $tf = 1$	1637	19188/2611471
discarding tf ≤ 2	1068	18050/1698226
discarding tf ≤ 3	869	17453/1379030

- □ Total number of documents: 1607
- □ Sparsity in every preprocessing step: 99%
- I select the preprocessing configuration "discarding tf <= 2": resulting a "text matrix" with 1068×1607 entries



Text to Vector

- $\boxdot D = \{d_1, \ldots, d_n\} \text{set of documents.}$
- □ $T = \{t_1, ..., t_m\}$ dictionary, i.e., the set of all different terms occurring in Quantnet.
- □ tf(d, t) absolute frequency of term $t \in T$ in document $d \in D$.
- □ $idf(t) \stackrel{\text{def}}{=} \log(|D|/n_t)$ inverse document frequency, with $n_t = |\{d \in D | t \in d\}|.$
- □ $w(d) = \{w(d, t_1), \dots, w(d, t_m)\}, d \in D$ documents as vectors in a m-dimensional space.
- \therefore $w(d, t_i)$ calculated by a weighting scheme.



Weighting scheme, Similarity, Distance

□ Salton et al. (1994): the tf-idf – weighting scheme w(d, t) for $t \in T$ in $d \in D$:

$$w(d,t) = \frac{tf(d,t)idf(t)}{\sqrt{\sum_{j=1}^{m} tf(d,t_j)^2 idf(t_j)^2}}, m = |T|$$

 \Box (normalized tf-idf) Similarity S of two documents

$$S(d_1, d_2) = \sum_{k=1}^m w(d_1, t_k) \cdot w(d_2, t_k) = w(d_1)^\top w(d_2)$$

□ A frequently used distance measure is the Euclidian distance:

$$dist_d(d_1, d_2) \stackrel{\text{def}}{=} \sqrt{\sum_{k=1}^m \{w(d_1, t_k) - w(d_2, t_k)\}^2}$$



Example 1: Shakespeare's tragedies

Let $D = \{d_1, d_2, d_3\}$ be the set of documents/tragedies:

Document 1: Hamlet

Document 2: Julius Caesar

Document 3: Romeo and Juliet



Vector Space Model (VSM)

now give sha night bathasan england 3 ust beauti horatio we are all here. See the set of t brutus Wi And double wind both perceiv hark scene bring bring COME queen comparison of the second secon vers laurenc unlucius And the second s mlet seek friar to seek friar to seek friar to seek friar can nay fellow gentleman keep hous look well

Figure 9: Wordcloud of all words (tf $\geq = 5$) in this 3 tragedies

Quantnet Basics



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Example 1: Shakespeare's tragedies



(among 100 most frequent)

 $T = \{art, bear, call, day, dead, dear, death, die, eye, fair, father, fear, friend, god, good, heart, heaven, king, ladi, lie, like, live, love, make, man, mean, men, must, night, queen, think, time \}$ $= \{t_1, \dots, t_{32}\}$





Figure 11: Weighting vectors of the 3 tragedies in a radar chart



Example 1: Shakespeare's tragedies

With the weighting vectors (32 special terms) above we get the similarity matrix:

$$M_S = \begin{pmatrix} 1 & 0.64 & 0.63 \\ 0.64 & 1 & 0.77 \\ 0.63 & 0.77 & 1 \end{pmatrix}$$

And the distance matrix:

$$M_D = \begin{pmatrix} 0 & 0.85 & 0.87 \\ 0.85 & 0 & 0.68 \\ 0.87 & 0.68 & 0 \end{pmatrix}$$



Example 1: Shakespeare's tragedies

With the weighting vectors (of all 5521 terms) in normalized TF-form we get the similarity matrix:

$$M_S = \begin{pmatrix} 1 & 0.39 & 0.46 \\ 0.39 & 1 & 0.42 \\ 0.46 & 0.42 & 1 \end{pmatrix}$$

And the distance matrix:

$$M_D = \begin{pmatrix} 0 & 1.10 & 1.04 \\ 1.10 & 0 & 1.07 \\ 1.04 & 1.07 & 0 \end{pmatrix}$$





Figure 12: Outlook for the t-SNE projection into 2 dimensions
Quantnet Basics

Basic VSM

- \Box vertical vector *d*, indexed by terms Document representation
- matrix $D = [d_1, \ldots, d_n]$ Document corpus representation, also called "term by document" matrix
- ⊡ considering linear transformations *P* we get a general similarity $S(d_1, d_2) = (Pd_1)^{\top} (Pd_2) = d_1^{\top} P^{\top} Pd_2$
- \boxdot every mapping *P* defines another *VSM*
- \square $M_S = D^{\top}(P^{\top}P)D$ similarity matrix



Example 2: tf and tf-idf similarities in BVSM

- . with $P = I_m$ and $d = \{tf(d, t_1), \dots, tf(d, t_m)\}^\top$ we get the classical tf-similarity: $M_S^{tf} = D^\top D$
- . with diagonal $P(i, i)^{idf} = idf(t_i)$ and $d = \{tf(d, t_1), \dots, tf(d, t_m)\}^\top$ we get the classical tf-idf-similarity: $M_S^{tf-idf} = D^\top (P^{idf})^\top P^{idf} D$



Drawbacks of BVSM

- □ Uncorrelated/orthogonal terms in the feature space
- Documents must have common terms to be similar
- □ Sparseness of document vectors and similarity matrices

Question

⊡ How to incorporate information about semantics?

Solution

- □ Using statistical information about term-term correlations
- Semantic smoothing



Generalized VSM – term-term correlations

- $\ \, \boxdot \ \, S(d_1,d_2)=(D^\top d_1)^\top (D^\top d_2)=d_1^\top D D^\top d_2 \text{the GVSM} \\ \text{similarity}$
- $\ \, \boxdot \ \, M_S = D^\top (DD^\top) D \text{similarity matrix}$
- DD[⊤] term by term matrix, having a nonzero *ij* entry if and only if there is a document containing both the *i*-th and the *j*-th terms
- terms become semantically related if co-occuring often in the same documents
- also known as a dual space method (Sheridan and Ballerini, 1996)
- when there are less documents than terms dimensionality reduction



Generalized VSM – Semantic smoothing

- More natural method of incorporating semantics is by directly using a semantic network
- ⊡ (Miller et al., 1993) used the semantic network WordNet
- Term distance in the hierarchical tree provided by WordNet gives an estimation of their semantic proximity
- (Siolas and d'Alche-Buc, 2000) have included the semantics into the similarity matrix by handcrafting the VSM matrix P

$$\square$$
 $M_S = D^{\top}(P^{\top}P)D = D^{\top}P^2D$ – similarity matrix



LSA – Latent Semantic Analysis

- □ LSA measures semantic information through co-occurrence analysis (Deerwester et al., 1990)
- : Technique singular value decomposition (SVD) of the matrix $D = U \Sigma V^{\top}$
- $\square P = U_k^\top = I_k U^\top \text{projection operator onto the first } k$ dimensions

$$\square M_S = D^{\top} (UI_k U^{\top}) D - \text{similarity matrix}$$

□ It can be shown: $M_S = V\Lambda_k V^{\top}$, with $D^{\top}D = V\Sigma^{\top}U^{\top}U\Sigma V^{\top} = V\Lambda V^{\top}$ and $\Lambda_{ii} = \lambda_i = \sigma_i^2$ eigenvalues of V; Λ_k consisting of the first k eigenvalues and zero-values else.



3 Models for the QuantNet

- Models BVSM, GVSM and LSA
- Dataset the whole Quantnet
- ☑ Documents 1607 Quantlets





Figure 13: Heat map with 2 Dendrograms of the BVSM SimMatrix Quantnet Basics





Figure 15: Heat map with 2 Dendrograms of the LSA SimMatrix Quantnet Basics

Sparseness results

	BVSM	GVSM	LSA
Sparseness TD Matrix	0.99	0.74	0.03
Sparseness Sim Matrix	0.74	0.08	0.05

Table 1: Model Performance regarding the sparseness of the "term by document"-matrix and the similarity matrix in the appropriate models.



Conclusion

- Different weighting scheme approaches and Vector Space Models allow adapted Similarity based Knowledge Discovery
- Incorporating term-term Correlations and Semantics significantly improves the comparison performance
- Similarity and Distance available for Clustering and extended Visualization



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Data Mining: DM

DM is the computational process of discovering/representing patterns in large data sets involving methods at the intersection of **artificial intelligence**, **machine learning**, **statistics**, and **database systems**.

- 1. Numerical DM
- 2. Visual DM
- 3. Text Mining

(applied on considerably weaker structured text data)



Text Mining

Text Mining or **Knowledge Discovery** from **Text** (KDT) deals with the machine supported analysis of text (Feldman et al., 1995).

It uses techniques from:

- □ Information Retrieval (IR)
- Information extraction
- ☑ Natural Language Processing (NLP)

and connects them with the methods of DM.



Text Mining II

Text Mining offers more models and methods like:

Classification

- Clustering
- □ Latent Dirichlet Allocation (LDA) topic model

• TopicTiling

They are worth being researched and applied to the Quantnet.



Index Term Selection I

Goal: decrease the number of words for indexing, so that only the selected keywords describe the documents (Deerwester et al., 1990; Witten et al., 1999)

A simple method for keyword extracting is based on their entropy. $\forall t \in T$ the entropy is defined:

$$W(t) = 1 + \frac{1}{\log_2 |D|} \sum_{d \in D} P(d, t) \log_2 P(d, t),$$

with
$$P(d, t) = \frac{tf(d, t)}{\sum_{l=1}^{n} tf(d_l, t)}$$



Index Term Selection II

The entropy as a measure of the importance of a word in the given domain context:

W(t) is high \Rightarrow prefer this t as index.

An index term selection method (fixed number of index terms) is discussed in "*Experiments in Term Weighting and Keyword Extraction in Document Clustering*" (Borgelt et al., 2004).



Similarity, Distance, Data Mining – Overview

- 1. Find a formal representation of the Quantlets
- 2. Find a similarity measure on the space of Quantlets
- 3. Afterwards the construction of a distance measure is simple:

$$distance(x, y) = \sqrt{sim(x, x) + sim(y, y) - 2 \cdot sim(x, y)}$$

Having similarity and distance \Rightarrow vast amount of Data Mining, Text Mining and Visualization technics.



Distance measure

A frequently used distance measure is the Euclidian distance:

$$dist_d(d_1, d_2) \stackrel{\text{def}}{=} dist\{w(d_1), w(d_2)\} \stackrel{\text{def}}{=} \sqrt{\sum_{k=1}^m \{w(d_1, t_k) - w(d_2, t_k)\}^2}$$

It holds for tf-idf:

$$\cos \phi = \frac{x^{\top} y}{|x| \cdot |y|} = 1 - \frac{1}{2} \operatorname{dist}^2 \left(\frac{x}{|x|}, \frac{y}{|y|} \right),$$

where $\frac{x}{|x|}$ means $w(d_1)$, $\frac{y}{|y|}$ means $w(d_2)$ and $\cos \phi$ is the angle between x and y.

3 Models on 3 Datasets

- Models BVSM, GVSM and LSA
- Datasets 2 books, 1 project from Quantnet
- Project 1 TEDAS: Tail Event Driven Asset Allocation (micro size - 4 Qlets)
- Book 1 BCS: Basic Elements of Computational Statistics (low size - 48 Qlets)
- Book 2 SFE: Statistics of Financial Markets (medium size - 337 Qlets)





Figure 16: Model characteristics of TEDAS

Quantnet Basics



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Figure 17: Quantiles of similarity values of 3 models on TEDAS

☑ Blue dots – BVSM; Green line – GVSM; Red line – LSA





Figure 18: Model characteristics of BCS





Figure 19: Quantiles of similarity values of 3 models on BCS

□ Blue dots – BVSM; Green line – GVSM; Red line – LSA





Figure 20: Model characteristics of SFE







Blue dots – BVSM; Green line – GVSM; Red line – LSA

Quantnet Basics



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Sparseness results

	TEDAS	BCS	SFE	MVA*	STF*	SFS*
BVSM	8	504	108668	75424	44576	17146
GVSM	8	0	96940	71464	44204	16612
LSA	8	262	84262	65712	43952	15400
Matrix Dim	16	2304	113569	77841	45369	18225

Table 2: Model Performance regarding the number of zero-values in the similarity matrix. MVA*, STF* and SFS* were additionally examined.



Appendix 7-16 BVSM - Histogram GVSM - Histogram LSI - Histogram 100 8 8 0.0 62 0.8 68 02 0.8 similarity values of QNet similarity values of GNet similarity values of GNet **BVSM** - Similarity Heat map GVSM - Similarity Heat map LSI - Similarity Heat map 0.8 S. - 0.4

Figure 22: Model characteristics

0.0



Appendix



Figure 23: Quantiles of similarity values of 3 models

□ Blue dots – BVSM; Green dots – GVSM; Red line – LSA

