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AN INCENTIVE-COMPATIBLE EXPERIMENT ON PROBABILISTIC INSURANCE AND IMPLICATIONS FOR AN INSURER'S SOLVENCY LEVEL

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Abstract

This article is the first to conduct an incentive-compatible experiment using real monetary payoffs to test the hypothesis of probabilistic insurance, which states that willingness to pay for insurance decreases sharply in the presence of even small default probabilities as compared to a risk-free insurance contract. In our experiment, 181 participants state their willingness to pay for insurance contracts with different levels of default risk. We find that the willingness to pay sharply decreases with increasing default risk. Our results, hence, strongly support the hypothesis of probabilistic insurance. Furthermore, we study the impact of customer reaction to default risk on an insurer's optimal solvency level using our experimentally obtained data on insurance demand. We show that an insurer should choose to be default-free rather than having even a very small default probability. This risk strategy is also optimal when assuming substantial transaction costs for risk management activities undertaken to achieve the maximum solvency level.

INTRODUCTION

After the financial crisis of 2008, financial services customers became highly concerned about the safety of financial products. The default risk inherent in such contracts has become a driving factor of purchase decisions, a situation highlighted by

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the emergence of financial strength ratings for financial services providers.¹ In fact, there is ample empirical evidence that awareness of default risk has an influence on consumers' insurance purchase behavior. Experimental research by Wakker, Thaler, and Tversky (1997), Albrecht and Maurer (2000), and Zimmer, Schade, and Gründl (2009) show that people dislike insurance contracts with default risk and that insurance demand is very sensitive to the insurer's level of default risk. These studies demonstrate that people will purchase an insurance contract that has the possibility of defaulting only if the insurance premium is substantially reduced compared to a default-free contract. Moreover, Zimmer, Schade, and Gründl (2009) find that there are a considerable number of consumers who will refuse to buy insurance at any level of default risk.

The very pronounced sensitivity of individuals' maximum willingness to pay, that is, the insurance premium that makes individuals indifferent between purchasing insurance and not purchasing insurance, that has been elicited in experiments cannot be plausibly explained by expected utility theory. Instead, Wakker, Thaler, and Tversky (1997) propose cumulative prospect theory, put forward by Tversky and Kahneman (1992), to explain this drop in willingness to pay caused by only small increments in the default probability. They coined the term "probabilistic insurance" for insurance contracts that have a nonzero probability of default. While existing experimental evidence and survey data support their theory, a rigorous incentivecompatible test of probabilistic insurance is still missing in the literature. This gap motivates our first research question of whether the hypothesis of probabilistic insurance is supported by experimental evidence in an experimental setting suited to incentivize truthful preference revelation and allowing for the implementation of high financial stakes. To this end, we employ features of the experimental designs by Bolle (1990) and Schade, Kunreuther, and Koellinger (2012) and modify them to integrate a default risk. Most importantly, our experiment is carried out in the laboratory and reveals policyholders' willingness to pay for insurance with default risk using large stakes of real money. Participants in this experiment stated their maximum willingness to pay for four different insurance contracts that only differed with respect to their default probability (0, 1, 2, and 3 percent, respectively).

We find that in the presence of default risk, individuals either refuse to purchase insurance altogether or they demand a considerable reduction in the insurance price compared to a default-free situation. For example, while in the case of the defaultfree insurance contract, 71 percent of the participants were willing to pay at least the actuarially fair premium, in the case of the insurance contract with a default risk of 3 percent, 50 percent of the participants were not willing to pay the actuarially fair premium. The median willingness to pay decreases from \in 54 for a default-free contract to \in 29 for a contract with 3 percent default probability (this compares to actuarially fair premiums of \in 40 and \in 38.80, respectively). This strong reduction in willingness to pay in the presence of only small default probabilities underscores how sensitively individuals react to only small increases in default risk when purchasing

¹See AMB Credit Reports—Consumer (www.ambest.com/sales/AMBCreditReportsConsumer/default.asp).

insurance. Our results, hence, strongly support the hypothesis of probabilistic insurance.

Our second research question is motivated by empirical evidence suggesting that the relationship between default risk and consumers' willingness to pay has important implications for financial services firms. Epermanis and Harrington (2006) observe a significant reduction of insurance demand in the year of and the year following a rating downgrade for the U.S. property-liability insurance market. Eling and Schmit (2012) find a similar relationship for the German insurance market, although to a somewhat lesser degree. Sommer (1996) and Cummins and Danzon (1997) show that a firm's financial distress is accompanied by a decrease in insurance premium income and vice versa. It has thus become crucial for financial services firms to take into consideration consumers' reaction to default risk when pricing products and managing risk. There exist several theoretical approaches to optimal risk management that incorporate the risk sensitivity of policyholders (see Doherty and Tinic, 1981; Rees, Graveller, and Wambach, 1999; Gründl and Schmeiser, 2002; Zanjani, 2002; Gründl, Post, and Schulze, 2006; Froot, 2007). However, all these approaches encounter the same problem, namely, a lack of empirical evidence on actual willingness to pay for insurance contracts when there is a default risk. We seek to fill this gap by developing a normative model of optimal risk management that accounts for empirically validated policyholders' reaction to the insurer's safety level and derive the shareholder value-maximizing solvency level of an insurance company when consumers are fully aware of the insurance contracts' default risk.

Our shareholder value model is based on Zanjani's (2002) model. To obtain empirically validated insurance demand curves, we use the data from our experiments. We find that the optimal safety level is a corner solution. Shareholder value will be maximized by choosing a default probability of zero, a result mainly driven by the overproportional increase in demand when the insurer chooses to be default-free rather than having even a very small default probability.² Insurer safety is, therefore, not only an effective means of attracting clients; it also contributes substantially to shareholder value.

We have three reasons for believing that a controlled laboratory experiment is the best way to empirically study individuals' willingness to pay for insurance with default risk. First, it allows us to conduct a clean test of the theory of probabilistic insurance in a controlled environment where individuals have full information on the loss distribution and the insurer's default risk. We can thereby prevent effects stemming from confounding circumstances encountered in reality, where individuals might act under ambiguity rather than risk. Second, it is difficult or even impossible to control for consumer knowledge and manipulate the level of default risk in other types of empirical studies. Third, the experimental approach enables us to measure

²We are fully aware that in the "real" world the possibility of a default cannot be completely eliminated due to the prohibitively high costs of the risk management necessary. However, an insurance company with a default probability very close to zero will be viewed by consumers as essentially default-free (see, e.g., Wakker, Thaler, and Tversky, 1997).

willingness to pay for insurance with default risk isolated from confounding variables, such as insurer reputation or size.

Our article consists of two parts, each of which is concerned with one of our two research questions. While the first part (the "Behavioral Theory and Hypothesis" section to "Results From the Experiment: Willingness to Pay and Demand Curves" section) describes our incentive-compatible test of probabilistic insurance, the second part (the "Optimal Safety Level of an Insurer" section) analyzes the optimal solvency level of a shareholder value-maximizing insurance company in the presence of policyholders whose willingness to pay for insurance depends on the company's default risk. In the "Discussion" section, we discuss our findings, and draw conclusions in the last section.

BEHAVIORAL THEORY AND HYPOTHESIS

In economic analysis, expected utility theory has been long established as the standard model of individuals' decision behavior. For the case of insurance, it states that a risk-averse individual is willing to purchase insurance at a premium above the expected value of indemnity payments in order to reduce his risk exposure (Mossin, 1968; Smith, 1968; Schlesinger, 1981, 2000). Expected utility theory implies that if there is a small default probability of the insurance contract, this will only marginally reduce an individual's willingness to pay for such a contract. Doherty and Schlesinger (1990) show that while the presence of default risk in an insurance contract does alter the demand for insurance in an expected utility framework, it does not necessarily reduce the demand. However, experimental studies have found that if there is a nonzero probability of contract nonperformance, individuals' willingness to pay decreases sharply (Wakker, Thaler, and Tversky, 1997; Albrecht and Maurer, 2000; Zimmer, Schade, and Gründl, 2009). As Wakker, Thaler, and Tversky (1997) show, this behavior cannot be explained within the paradigm of expected utility theory for common utility functions and even extreme degrees of risk aversion.³ The reason for such a behavior seems to lie in individuals' perception of risk. A coherent theory on what drives individuals' decisions under risk and what role the perception of risk plays in this process has been presented by Tversky and Kahneman (1992) and is known as cumulative prospect theory. According to this theory, individuals assign subjective (and cumulative) probability weights to outcomes, which differ from the objective probabilities. Fringe events with a small objective probability are assigned a probability weight much larger than the objective probability, whereas mediumranked events and/or those with a high objective probability are assigned a probability weight smaller than the objective probability. Wakker, Thaler, and Tversky (1997) apply this insight to the purchase of probabilistic insurance, that is, an insurance contract that bears a nonnegative default risk. In this context, cumulative prospect theory predicts that individuals will weigh the small probability of contract nonperformance very highly, that is, assign a weight that is larger than the objective probability, and hence substantially reduce their willingness to pay for such a contract.

³For details see the discussion on Equation (1) below.

Wakker, Thaler, and Tversky (1997, p. 12) show that under the hypothesis of expected utility, the ratio of the willingness to pay for probabilistic insurance and the willingness to pay for default-free insurance is approximately 1 - dp%⁴.

$$WTP_{dp\%} \approx (1 - dp\%) WTP_{dp=0\%},\tag{1}$$

where $WTP_{dp\%}$ denotes the willingness to pay for an insurance contract with a default probability of dp%, and $WTP_{dp=0\%}$ denotes the willingness to pay for a default riskfree contract. Under expected utility theory, also, the ratio of willingness to pay and the actuarially fair premium adjusted by the default probability is approximately constant for the default probabilities considered here. In contrast, the theory of probabilistic insurance suggests that the willingness to pay for an insurance contract with default risk drops by more than the adjustment for the default probability in the actuarially fair premium.⁵ For our analysis of individuals' willingness to pay for contracts with different levels of default risk, we, therefore, hypothesize the following:

Hypothesis: For small default probabilities, the ratio of willingness to pay and the actuarially fair insurance premium decreases with increasing default risk.⁶

EXPERIMENT

The goal of the laboratory experiment is to elicit individuals' willingness to pay for several theft insurance contracts, each having a different level of default risk. We chose a framed experiment to make it easier for participants to understand the decision they had to make. Insurance decisions, in particular, are often difficult to

⁴See Wakker, Thaler, and Tversky (1997, p. 12, Theorem 2.2). This result holds across all specifications of utility functions as well as risk aversion parameters used by Wakker, Thaler, and Tversky (1997, p. 13, Table 2, where the examples refer to a 1 percent default probability of an insurer). We extended Wakker, Thaler, and Tversky's calculations to the prominent power utility function (exhibiting constant relative risk aversion) (see, e.g., Harrison and Rutström, 2008, p. 69), using the experimentally elicited range of risk aversion parameters (see Harrison and Rutström, 2008, p. 66). In addition, we did the calculations for the default probabilities of 2 and 3 percent, and observed the property given by Equation (1) in all settings.

⁵The reason lies in the application of (cumulative) decision weights in cumulative prospect theory instead of objective probabilities in an expected utility framework: the willingness to pay within the cumulative prospect theory framework can, in principle, be derived from Equation (1) by substituting the default probability by a decision weight. In line with cumulative prospect theory, this decision weight is greater than the objective probability for low (and high) objective (fringe) probabilities. Intermediate as well as medium-sized probabilities are substituted by decision weights that are smaller than the objective probabilities. For more details see Wakker, Thaler, and Tversky (1997, pp. 15–17, in particular Theorem 3.2).

⁶It is beyond the scope of this article to provide a proof of this effect over the entire interval of potential probability values. However, default probabilities are typically small, and we look at a maximum of 3 percent where we are clearly in the domain of this effect.

understand,⁷ and providing a context to participants helps facilitate the decision process. Moreover, if there are any special perceptions and emotions that pertain to insurance decisions (which is plausible because safety concerns are "special" in the goals they invoke; see Krantz and Kunreuther, 2007), we would not capture them in a "clinical" that is, context-free frame but only in a framed choice. The results of this experiment also allow us to test the theory of probabilistic insurance by Wakker, Thaler, and Tversky (1997). We wanted to ensure that subjects were involved and interested in the experimental tasks, and in particular that they were incentivized to state their true or real willingness to pay. Holt and Laury (2002, 2005) demonstrate the importance of incentivization of participants in an experiment. Therefore, all the decisions participants made in our experiment had real-money consequences.

Experimental Design

Our experiment adapts basic features of Schade, Kunreuther, and Koellinger's (2012) design (for the complete experimental instructions, see Appendix A^8). Similar to the exact probabilities treatment in that study, our participants were asked to imagine that they had inherited a coin collection worth €800. Each participant was given a picture of the collection, which later would serve as a receipt. Subjects were informed that only one person out of all those participating in the experiment would be given a real coin collection⁹ and that this person would receive the value of the collection (€800) in cash. All other participants would receive a forgery. The person owning the real coin collection—and thus the €800—would be chosen at random at the end of the experiment. Each participant was also told that the real collection was threatened by a 5 percent risk of theft. To help them better understand this concept, participants were told that a 5 percent chance of theft is comparable to the chance of drawing ball 1 out of 20 numbered balls in a bingo cage.¹⁰

Subjects were next offered full insurance to protect against a possible loss of the \in 800. It was pointed out that only the owner of the real coin collection would actually pay for the insurance contract; all other insurance purchase decisions would be considered hypothetical.

⁷This especially pertains to the small probabilities concerned in those choices and the understanding of their meaning (Kunreuther, Novemsky, and Kahneman, 2001; Schade, Kunreuther, and Koellinger, 2012) as well as the combinations of large potential consequences and small losses (Kunreuther et al., 2002).

⁸A second part of the experiment (coin collection B) employed a different method of preference elicitation, namely, pairwise comparison of insurance contracts with given default probabilities and prices. When making their decisions in Part A, the participants did not know what decisions they would have to make in Part B. The protocol for Part B is available from the authors upon request.

⁹This "randomized reward scheme" was first proposed and demonstrated to work by Bolle (1990). The Schade, Kunreuther, and Koellinger (2012) study was its first implementation in a realistic insurance scenario.

¹⁰See Slovic et al. (1977) for an early application of an urn game in the insurance context.

To elicit maximum willingness to pay, we employed Schade and Kunreuther's (2001) secret price mechanism (see also Wang, Venkatesh, and Chatterjee, 2007; Schade, Kunreuther, and Koellinger, 2012), which is a modification of the standard Becker-DeGroot-Marschak (BDM) mechanism (Becker, DeGroot, and Marschak, 1964).¹¹ This modification is necessary to deal with the situation of multiple probabilities for which the original BDM mechanism is known to cause problems (Safra, Segal, and Spivak, 1990). Subjects were asked to state their maximum willingness to pay for the respective insurance contract. They were not given any information about the selling price but were instead informed that the seller had already set a price (the "secret price"), which is written on an index card within a sealed envelope. The envelope was shown to the participants. Subjects were further told that if their buying price was equal to or higher than the secret selling price, they would be able to purchase the theft insurance for the secret price. However, if their maximum willingness to pay was lower than the secret price, they would be refused insurance protection. We made it clear that it would be in the participants' best interest to state their true maximum willingness to pay and advised them to do so from different perspectives.¹² If they stated a price lower than their maximum willingness to pay, they might not be able to purchase insurance even though they would have been willing to buy protection at a higher price than the amount stated. If they stated a price higher than their maximum willingness to pay, they might have to pay this higher price (assuming they were the owner of the real coin collection) even though they would not have been willing to do so.

Participants were then asked to indicate, on a computer screen, their maximum willingness to pay for each of four alternative contracts.¹³ All contracts were displayed on the computer screen at the same time, and the order of the contracts was the same for everyone. Participants were informed that each contract had a different level of default risk (0, 1, 2, or 3 percent default probability¹⁴) but that in all other

¹¹Note that the argument for incentive compatibility of the secret price mechanism is, however, the same as made and mathematically proven by Vickrey (1961). Basically, it is essential that the probability density of the subjective distribution of the secret price is nonzero in all relevant parts.

¹²Individuals might form beliefs about the location of the secret price finding some intervals more plausible than others, but they can never be certain enough (without any such information) to exclude reasonable price intervals. And if the probability density function of an individual's belief about the distribution of the secret price is nonzero throughout an interval of reasonable prices, this mechanism is fully incentive compatible.

¹³The computer-assisted part of the experiment was programmed and conducted with z-Tree software (Fischbacher, 2007).

¹⁴To specify the insurer's default situation, we decided to use numeric default probabilities instead of, for example, insurer financial strength rating or issuer credit rating definitions provided by rating agencies. In a prestudy, we found that individuals overestimate default probabilities for verbal insurer rating definitions. For example, for an insurer rating definition by Standard & Poor's of BBB (i.e., good financial security characteristics), which corresponds to an actual annual default probability of 0.3 percent, individuals estimate the insurer's default probability to be 8 percent on average (median = 1 percent, standard deviation = 13 percent).

aspects, the insurance contracts were identical. Each contract had a secret price. Subjects were further told that one of the contracts would be chosen at random and that the stated price for this chosen contract would determine whether or not the person would purchase that particular insurance contract. Thus, participants should have been aware that each insurance purchase decision could be the relevant one, and thus constitute their only chance to buy theft insurance. Participants had no choice in the matter of which contract would be the relevant one for them.¹⁵ Figure 1 shows one example of the theft insurance contracts offered.

After all experimental sessions to elicit individuals' willingness to pay had been conducted in November and December 2007, we scheduled a further session in January 2008 in order to determine both the participant to whom the payoff from the experiment would be made in real terms and the amount of this real-money payoff.¹⁶ We invited all participants from the experiment to participate. In a first step, a random draw determined who would be eligible for obtaining the value of the coin collection from the experiment. The decision that the individual had made during the

FIGURE 1

Theft Insurance Contract

Risk Exposure	
Risk of theft	Loss of a coin collection valued at 800 Euro with a 5% probability of the ft; 95% probability of no the ft
Insurance contract 4:	
Insurance:	1-year theft insurance
Scope of indemnity	Loss due to theft of coin collection
Sum insured:	800 Euro
Default risk	3%, i.e., the insurer pays its valid claims in 97 out of 100 cases, and in 3 out of 100 cases the insurer does not pay!

Note: The figure shows an example of the theft insurance contracts offered. The reported contract has a 3 percent default probability.

¹⁵Using the random lottery incentive system, we ensure that all participants have an incentive to reveal their true maximum willingness to pay for each insurance contract. Because of money constraints for recruiting subjects, we could not use a between-subjects design. To obtain the same amount of data, we would have had to invite four times as many participants. For the validity of the random lottery incentive system, see, for example, Cubitt, Starmer, and Sugden (1998).

¹⁶We invited participants to an additional session in January 2008 because we needed to determine the participant who would get the real-money payoff. Due to the size of the laboratory, several sessions were needed to run the experiment with 181 participants. As all participants from all experimental sessions conducted in November and December 2007 were eligible for the real-money payoff, the final draw could not be made before January 2008. This means that discount rates might have been relevant to participants' decisions. However, the discount rate impacted all relevant payments, and therefore should not systematically distort the experimental results.

experiment was used to determine whether or not he or she would purchase theft insurance. The owner of the real coin collection drew one ball from a bingo cage with 20 balls to determine whether theft occurred. If theft occurred and the participant did not have an insurance contract, he lost the coin collection. If theft occurred and the participant had purchased insurance, the owner of the coin collection did a further random draw from a bingo cage to determine whether or not the insurance company would pay the claim.

We conducted 16 experimental sessions in November and December 2007. The number of subjects varied across the sessions, ranging from 4 to 14 with a total of 181 subjects. Participants were invited to take part through subject pools of the faculty of business and economics and the faculty of psychology of a major public university in Germany. The invitation explained that the experiment would last for about 75 minutes and that the amount that could be earned from participating would depend on decisions made and chance. However, all participants were guaranteed \in 4 remuneration. All subjects were seated in separate computer booths during the sessions. Table 1 provides some summary statistics about the sample.

RESULTS FROM THE EXPERIMENT: WILLINGNESS TO PAY AND DEMAND CURVES

Descriptive Analysis

Before providing a more formal analysis, we present some descriptive statistics on participants' reaction to default risk and their willingness to pay for insurance in Tables 2 and 3. Seven percent of the participants were unwilling to pay anything for

TABLE	1

Summary	V Statistics	About the	Subject	Pool	in	the	Experime	ent

	п	%
Gender		
Female	79	44
Male	102	56
Highest educational degree		
No high school degree	23	13
High school degree	112	62
University degree	45	25
Other	1	0
Occupation		
Student	117	65
Employee	28	15
Other	36	20
Field of study		
Economics/business administration	145	80
Other	36	20

Note: The table provides some summary statistics on the participants in the experiment (N = 181). Category "Other" was the default category in the "Field of study" and thus also comprises the 23 participants with no high school degree.

TABLE 2

Consumers' Reactions to Insurance With Default Risk

Participants who	Frequency (%)
Do not want to buy insurance (or willingness to $pay = 0$)	13 (7.2)
Demand insurance protection in general	168 (92.8)
of those	
Only accept a default-free insurance contract	6 (3.6)
Do not accept insurance contracts with 2% and 3% default risk	4 (2.4)
Do not accept insurance contracts with 3% default risk	18 (10.7)
Accept all levels of default risk	129 (76.8)
Show inconsistent behavior	11 (6.5)

Note: The first two rows show the portion of consumers unwilling or willing to purchase insurance (N = 181). Rows 4–7 report the fraction of individuals who generally demand insurance protection but only accept certain default levels.

TABLE 3

Consumers' Willingness to Pay

		Insurance	Contracts Wit	h a Default Pr	obability of
		0%	1%	2%	3%
Actuarially Fair Insura	nce Premium	€40	€39.6	€39.2	€38.8
Willingness to pay	Mean	€92	€69	€57	€46
	SD	€99	€81	€71	€71
Percentiles	25%	€30	€20	€15	€5
	50%	€54	€49	€40	€29
	75%	€100	€80	€72	€50
	90%	€222	€150	€125	€100

Note: The table reports the descriptive statistics of willingness to pay for all insurance contracts and those individuals who are generally willing to purchase insurance protection (N = 168).

insurance, regardless of the insurer's default situation. Of those who did want insurance protection, 3 percent refused to accept any default risk, 2 percent were willing to pay only for an insurance contract with 1 percent default risk, and 10 percent rejected the contract having 3 percent default risk but accepted all other levels of default risk. Six percent could not be categorized due to inconsistent behavior. For example, one person was willing to accept all levels of default risk but refused to buy a default-free contract. The biggest fraction of individuals (71 percent) was willing to purchase insurance at every level of default risk. The results further show that individuals who—in principle—accept default risk demand a considerable reduction in insurance premiums compared to their willingness to pay for a default-free contract. For example, individuals require a premium reduction of 9 percent (comparison of median values) when facing a 1 percent default probability.¹⁷ For a contract with 3 percent default probability, over 50 percent of the participants stated a price less than the expected claims payment (i.e., \in 38.80), whereas in the default-free case, only 29 percent were unwilling to purchase insurance for the price of the expected claims payment of \in 40.¹⁸ Comparing the relationship between willingness to pay and the actuarially fair premium, we find that the median willingness to pay decreases from well above the actuarially fair premium in case of a default-free insurance contract (\in 54 vs. a fair premium of \in 40) to an amount significantly below the fair premium in case of a 3 percent default probability (\notin 29 vs. a fair premium of \notin 38.80).

Regression Analysis

To provide a more formal test of probabilistic insurance, we conduct a regression analysis of individuals' willingness to pay. For every individual, we observe the willingness to pay for four contracts with different levels of default risk, resulting in a total of 724 observations. The data set contains several observations with zero willingness to pay. We account for this censoring in the distribution of willingness to pay by employing a Tobit regression model with random effects and a cutoff value of zero at the lower end of the distribution.

Our dependent variable is the ratio of an individual's willingness to pay for an insurance contract with a given default risk and the actuarially fair premium for the corresponding contract. Because of this standardization, we can compare the willingness to pay across different levels of default risk for a given individual. Furthermore, as probabilistic insurance predicts this ratio to be declining in the default probability, it allows for a straightforward test of whether the hypothesis of expected utility can be rejected with our experimental data. As we want to analyze the effect of default risk on the (relative) willingness to pay for insurance, we include dummies for each of the three insurance contracts that are exposed to default risk. The contract with zero default probability hence serves as a reference category.

We sequentially estimate three regression models, the results of which are reported in Table 4. The first two regressions use all the observations for all participants, whereas for the third regression we excluded those individuals whose willingness to pay was increasing in the contract's default risk. The main result from these three regressions is that the willingness to pay for insurance decreases in default probability.

The parameter estimates for the dummies for contracts with default risk are all negative and statistically significant at the 0.1 percent level. Consider, for example, the contract with a default probability of 3 percent. The ratio of willingness to pay to the actuarially fair premium decreases for that contract by 1.26 as compared to the

¹⁷In addition to mean values and standard deviations, we also report median values (or other percentiles). We focus our analysis on the median values because we observed right-skewed and fat-tailed distributions of willingness to pay.

¹⁸The latter result is in line with a study by Loubergé and Outreville (2001, p. 231). They report that around 70 percent of their 192 subjects were willing to buy an actuarially fair insurance contract for a loss occurring with a probability equal to or smaller than 5 percent.

TABLE 4

Regression of Individuals' Willingness to Pay for Probabilistic Insurance, Divided by the Actuarially Fair Premium

	(1)	(2)	(3)
Contract1 (3% dp)	-1.2565***	-1.2573***	-1.4924^{***}
	(-10.44)	(-10.44)	(-14.23)
Contract2 (2% dp)	-0.8625^{***}	-0.8632^{***}	-1.0783^{***}
	(-7.29)	(-7.29)	(-10.46)
Contract3 (1% dp)	-0.5792^{***}	-0.5798^{***}	-0.6883^{***}
,	(-4.91)	(-4.91)	(-6.72)
Female		-0.6168	-0.6421
		(-1.82)	(-1.77)
Degree		-0.1842	-0.2270
		(-1.18)	(-1.34)
Economics		-0.4996	-0.5658
		(-1.26)	(-1.32)
Willingness to take risks		0.0812	0.0511
0		(0.64)	(0.37)
Competence		-0.1077	-0.1051
		(-0.98)	(-0.89)
Optimism		-0.2141	-0.1854
		(-1.76)	(-1.35)
Constant	1.9855***	4.1059***	4.4484***
	(11.42)	(4.34)	(4.48)
Observations	724	724	664

Note: The table reports the regression results of respondents' willingness to pay for each of the four insurance contracts divided by the actuarially fair premium. The first two regressions use all the observations for all participants (N = 181). The third regression excludes those participants whose willingness to pay was increasing in the contract's default risk (N = 166). The variables Contract1 to Contract3 are dummy variables indicating the insurance contract. The contract with no default risk serves as the reference category. The variable Female is a binary variable indicating female respondents. The variable Degree represents the highest educational degree a respondent has attained. It is a category variable that ranges from 1 to 9, where higher values indicate a higher educational degree. The variable Economics is a dummy variable indicating students enrolled in an economics or business administration program. The variable Willingness to take risks is the respondent's self-assessed proneness to take risks, the variable Competence is the respondent's self-assessed competence in insurance-related questions, and the variable Optimism is the respondent's self-assessed degree of optimism. The self-assessments of Willingness to take risks, Competence, and Optimism were done on a Likert-scale from 1 to 7, where higher values indicate a higher degree of the respective attribute. The *t*-statistics are in parentheses. ***p < 0.001.

contract without default risk. Excluding those individuals whose willingness to pay increased with default risk and controlling for personal characteristics, the difference in ratios even amounts to 1.49. As the ratio of median willingness to pay for a default-free contract of \in 54 (Table 3) to the actuarially fair premium of \in 40 amounts to 1.35, this is a significant impact of default probability on participants' willingness to pay

for probabilistic insurance relative to the actuarially fair premium. This result strongly supports the hypothesis of probabilistic insurance.

We further include control variables for the respondents' socioeconomic characteristics. In particular, we include a dummy for female respondents, the respondents' highest educational degree, a dummy for students enrolled in an economics or business administration program, the respondents' self-assessed general willingness to take risks, as well as their optimism and their self-assessed competence in insurance-related questions. The results from that regression are reported in regression (2) in Table 4. The parameters for the variables indicating the different contracts are again negative and statistically significant.

The variables representing personal characteristics, however, do not have any significant influence on the outcome variable. On average, the overproportionally negative effect of an increase in the default risk on willingness to pay is independent of observable characteristics of the participants.

In a third regression we exclude those 15 individuals whose willingness to pay was increasing in default risk. Paying more for probabilistic insurance than for default-free insurance means preferring a stochastically dominated alternative, which violates the standard assumption of a monotonically increasing utility function (see Quirk and Saposnik, 1962). Such behavior could indicate that either participants did not understand the experimental task or they were not stating their real willingness to pay. The results from this regression are reported in column (3) of Table 4. The parameter estimates do not significantly differ from those in the first regressions.

Our hypothesis based on previous findings was that the ratio of willingness to pay and the actuarially adjusted insurance premium decreases with increasing default risk. The results from a set of regressions are robust across different specifications and strongly substantiate this hypothesis.

OPTIMAL SAFETY LEVEL OF AN INSURER

We analyze the optimal safety level of an insurance company using a single-period model of shareholder value maximization. This is a modified version of the model proposed by Zanjani (2002).¹⁹ We keep the model as simple as possible in order to focus on the effects stemming from insurance demand. We explain our model in some detail so as to clarify our system of notation as well as our underlying assumptions.

At the beginning of the period, shareholders invest equity capital E_0 , which is constant over the entire period, and Q policyholders pay insurance premiums $Q\pi$, which are invested within the company and serve as safety capital. Insurance demand depends on the insurance price as well as the default risk and is obtained from our experimental data, as will be discussed below. For the sake of simplicity and to match

¹⁹For related approaches, see, for example, Doherty and Garven (1986), Cummins and Sommer (1996), Cummins and Danzon (1997), Rees, Graveller, and Wambach (1999), and Gründl and Schmeiser (2002).

the experimental design discussed above, we assume independent and identically binomially distributed risks in a single line of business. Policyholder claims L will be settled at the end of the period. Shareholders favor a company policy that maximizes the net present value of their equity capital investment;²⁰ that is, they favor a (net) shareholder value (SHV) maximization. Assuming that the loss distribution is uncorrelated with financial asset prices, and further that the insurance company invests at the risk-free rate, we can write the shareholder value of the insurance company as follows:

$$SHV = Q\pi - \frac{1}{1 + r_f} E(L) + DPO(L; Y),$$
 (2)

where r_f denotes the risk-free rate of return, E(L) denotes the expected insured loss, Y is the terminal asset value of the insurer (= $(Q\pi + E_0)(1 + r_f)$), and DPO(L; Y) denotes the value of the default put option in the presence of shareholders' limited liability, that is, the value of the payments policyholders will not receive in the case of insolvency (Butsic, 1994).

Shareholder value thus arises from premium income, reflecting policyholder willingness to pay depending on the insurer's risk situation, minus the arbitrage-free value of the claims payment.²¹

Note that if there is information asymmetry between shareholders and policyholders, the insurer could increase risk after the contracts were signed (Smith and Stulz, 1985, p. 398), for example, by extracting equity capital from the firm. This would increase the default put option value and, by the same amount, shareholder value. In our model, policyholders cannot be cheated like this because of, for example, regulatory intervention. Instead, we assume—and this is in line with our experimental design—that policyholders receive the safety level originally promised. The insurer's decision variables are thus its safety level and the insurance premium π .

As equity capital cannot be adjusted (in the short run), given a certain defaultdependent premium income, additional risk management measures like purchasing reinsurance or financial derivatives may be necessary to achieve the desired (and promised) level of default risk. In our model, we calculate the value of those

²⁰For a discussion of the rationale of the objective function "maximize shareholder value," see Wilhelm (1989).

²¹This model is in line with Doherty's two-factor valuation model (Doherty, 1991, p. 234), or the similar approach by Froot and Stein (1998), in that the shareholder value, in principle, contains the valuation of systematic risk components as well as of idiosyncratic firm risk. The firm-specific risk situation influences firm value for its shareholders, in our case via the policyholder demand function. Lower demand for insurance due to higher firm risk can reduce shareholder value. This value reduction can be subsumed under "bankruptcy costs" (Stulz, 1996, p. 13). Therefore, it becomes rational for the insurer to engage in corporate risk management. For the importance of corporate risk management, see also Nocco and Stulz (2006).

necessary risk management (*RM*) measures as the difference between the actual shareholder value and the shareholder value under the promised level of default risk, that is,

$$RM_{dp\%} = SHV_{actual_dp\%} - SHV_{promised_dp\%}$$

where $dp \in \{0; 1; 2; 3\}$.²² Whenever the actual shareholder value is higher than the shareholder value under the promised level of default risk dp%, it means that the insurer's actual default risk is higher than the promised default risk, and additional risk management measures need to be taken. In the reverse case, the insurance company is safer than it needs to be and it can, for example, free up equity capital. We assume that these transactions come at a proportional cost *c*, so that the shareholder value after all necessary transactions equals

$$SHV_{ensured_dp\%} = SHV_{promised_dp\%} - c \cdot RM_{dp\%}.$$

Data

We use data from the experiment described above in determining the optimal safety level of an insurance company. Our "sample" insurance company has the following characteristics. The insurer operates in the market for property-liability insurance with a market size of 181 policyholders.²³ The price-demand functions for insurance contracts with different levels of default risk are derived from our experimentally obtained data. To estimate aggregate demand curves (or price-response curves)²⁴ from the willingness to pay data, we employed several parametric models commonly used in the literature.²⁵ The best model fit is obtained from the nonlinear model $q_{dp\%} = e^{\beta \pi + \gamma}$, where $q_{dp\%}$ characterizes the percentage of the sample willing to purchase theft insurance at the price of π . The parameters β and γ represent the coefficient estimates that are presented in Table 5. Parameter β describes the curvature of the demand function. Specifically, the price elasticity of demand is given by $\beta\pi$. The parameter γ determines the maximal number of market participants who are generally willing to purchase insurance, that is, those who are willing to purchase insurance for a price of zero. Specifically, e^{γ} is the percentage of the total market that is in principle willing to purchase insurance for a given default risk. In Figure 2 below, e^{γ} corresponds to the intercept of the *y*-axis.

²²Appendix B provides a more detailed description of how we determine the value of the necessary risk management measures.

²³Note that for the sake of simplicity, market size is determined by the number of participants in our experiment. Adjusting the model to any market size would not change the basic results under the assumption that the demand curve parameters are representative.

²⁴In a monopolistic market environment, the price-response curve equals the market-demand curve. See Phillips (2005, p. 38) for more details on the difference between price-response and demand curves.

²⁵See, for example, Phillips (2005) for an overview of price-response models. The results of all estimations are available from the authors upon request.

	Model	Parameter	Estimate	Std. Error	T-Ratio	R^2
Price-demand curves	$q_{0\%}$	β	-0.011	3.13E-04	-33.99	0.997
	.070	γ	-0.081	5.41E-03	-15.59	
	$q_{1\%}$	β	-0.014	3.8E-04	-38.53	0.996
	,1/0	γ	-0.086	1.20E-02	-7.15	
	$q_{2\%}$	β	-0.017	4.05E-04	-42.76	0.996
	12/0	γ	-0.095	1.11E-02	-8.60	
	$q_{3\%}$	β	-0.021	6.56E-04	-31.24	0.993
	.370	γ	-0.206	1.61E-02	-12.82	

TABLE 5

Aggregate Demand Curves

Note: The table reports the regression results of the estimated price-demand models for each default probability. The dependent variable is the percentage of the respective sample willing to purchase theft insurance contracts. The sample size for estimating the price-demand curves is 181 subjects for each contract type.

Figure 2 shows the estimated price-demand curves for each default probability. The figure clearly illustrates that the lower the default probability of an insurance contract, the higher the demand for it.

Results

We calculate an insurance company's optimal safety level and resulting shareholder value as illustrated in Figure B1 (Appendix B), using the price-demand curves we estimated for different levels of default risk. We report our results in Table 6 for an

FIGURE 2



Price-Demand Curves

Note: The figure shows the estimated price-demand curves for each default probability (*dp*). Demand is expressed as the percentage of the market size.

Contractually Agreed Default Fair π $q_{dp\%}$ Optimal $SHV_{actual Ap\%}$ Actual $SHV_{promised Ap\%}$ $RM_{dp\%}$ $RM_{dp\%}$ $SHV_{promised Ap\%}$ $RM_{dp\%}$ $SHV_{promised Ap\%}$ $RM_{dp\%}$ $RM_{dp\%$											
0 40 22 40 131 5,240 3,785.69 0.07 3,785.45 0.24 3,785.41 1 39.6 20 36 110 3,960 2,652.54 0.83 2,658.58 -6.04 2,658.58 2 39.2 17 31 99 3,069 1,948.16 1.79 1,958.18 -10.02 1,958.18 3 38.8 14 25 85 2,125 1,235.23 3.41 1,202.14 13.09 1,219.52 Note: The table provides the insurer's optimal safety 14 25 85 2,125 1,235.23 3.41 1,222.14 13.09 1,219.52 Note: The table provides the insurer's optimal safety 14 25 85 2,125 1,235.23 3.41 1,202.14 13.09 1,219.52 Note: The table provides the insurer's optimal safety 14 25 85 2,125 1,235.23 3.41 1,20.26, a risk-free interest rate of motion so folicyholders willing to purchase the specific insurance contract. SHV actual Apx, SHV provised Apx, and SHV ensured Apx, represent situation-specific insurred at price management.	Contractually Agreed Default Probability (Safety Level) (%)	Fair π in \in	$q_{dp\%}$ (%)	Ø	Optimal π in \in	Qπ	SHV _{actual} _dp% in €	Actual dp (%)	SHV _{promised_dp%} in €	$RM_{dp\%}$ in ${inom{\epsilon}}$	SHV _{ensured_dp%} in €
1 39.6 20 36 110 3,960 2,652.54 0.83 2,658.58 -6.04 2,658.58 2 39.2 39.2 17 31 99 3,069 1,948.16 1.79 1,958.18 -10.02 1,958.18 38.8 14 25 85 2,125 1,235.23 3.41 1,222.14 13.09 1,219.52 Note: The table provides the insurer's optimal safety level with constant equity capital $E_0 = $ €400, a cost rate $c = 20\%$, a risk-free interest rate $r_f = 10\%$, and a market size of 181 potential policyholders. Q represents the number of policyholders willing to purchase the specific insurance contract at price π . <i>qp</i> is the default probability of the respective insurance contract. <i>SHV</i> _{actual Ap\%} , <i>SHV</i> _{promised Ap\%} , and <i>SHV</i> _{ensured Ap\%} , represent situation-specific insurance to respective insurance contract. <i>SHV</i> _{actual Ap\%} , sath <i>SHV</i> _{ensured Ap\%} , represent situation-specific insurer shareholder values. <i>RM</i> _{dp\%} is the arbitrage-free value of risk management.	0	40	22	40	131	5,240	3,785.69	0.07	3,785.45	0.24	3,785.41
2 39.2 17 31 99 3,069 1,948.16 1.79 1,958.18 -10.02 1,958.18 38.8 14 25 85 2,125 1,235.23 3.41 1,222.14 13.09 1,219.52 Note: The table provides the insurer's optimal safety level with constant equity capital $E_0 = \epsilon 400$, a cost rate $c = 20\%$, a risk-free interest rate $r_f = 10\%$, and a market size of 181 potential policyholders. Q represents the number of policyholders willing to purchase the specific insurance contract at price π . <i>dp</i> is the default probability of the respective insurance contract. SHV _{actual Ap%} , SHV _{promised Ap%} , and SHV _{ensured Ap%} represent situation-specific insurer shareholder values. $RM_{dp\%}$ is the arbitrage-free value of risk management.	1	39.6	20	36	110	3,960	2,652.54	0.83	2,658.58	-6.04	2,658.58
$\frac{3}{r_f} = 10\%, and a market size of 181 potential policyholders. Q represents the number of policyholders willing to purchase the specific insurance contract at price \pi. qp is the default probability of the respective insurance contract. SHVactual-dp%, SHVpromised-dp%, and SHVensured-dp% represent stuation-specific insurance structures shareholder values. RMdp% is the arbitrage-free value of risk management.$	2	39.2	17	31	66	3,069	1,948.16	1.79	1,958.18	-10.02	1,958.18
Note: The table provides the insurer's optimal safety level with constant equity capital $E_0 = \varepsilon 400$, a cost rate $c = 20\%$, a risk-free interest rate $\tau_f = 10\%$, and a market size of 181 potential policyholders. Q represents the number of policyholders willing to purchase the specific insurance contract at price π . dp is the default probability of the respective insurance contract. $SHV_{actual-Ap\%}$, $SHV_{promised-Ap\%}$, and $SHV_{ensured-Ap\%}$ represent situation-specific insurance tract at price insure shareholder. RM $d_{ap\%}$ is the arbitrage-free value of risk management.	3	38.8	14	25	85	2,125	1,235.23	3.41	1,222.14	13.09	1,219.52
	<i>Note</i> : The table provides the insurer $r_f = 10\%$, and a market size of 181 p contract at price π . <i>dp</i> is the default situation-specific insurer sharehold	r's optimal s octential poli probability er values. R	afety l cyholc of the M _{dp%} i	evel v lers. (respe s the	vith const 2 represen ctive insu arbitrage-	ant equ ts the n rance co free val	ity capital E_0 = umber of polic ontract. SHV_{act} ue of risk man	= €400, a yholders _{ual_dp%} , SH agement.	$\cos t$ rate $c = 20\%$ willing to purcha $V_{promised_dp\%}$, and), a risk-fr ise the spe SHV _{ensure}	ee interest rate cific insurance d_dp% represent

Table 6 Insurer's Optimal Safety Level initial equity capital of \notin 400, a risk-free interest rate of $r_f = 10$ percent, and a cost rate for risk management of c = 20 percent. The optimal prices are calculated using the different demand functions that refer to the respective default probabilities. The generated premium income, together with the equity capital endowment, lead to a specific "actual" default probability that is either higher (for dp = 0 and 3 percent) or lower (for dp = 1 and 2 percent) than the contractually agreed default probability. So, risk management must either be additionally purchased (for dp = 0 and 3 percent) or can be reduced (for dp = 1 and 2 percent), which explains the different signs in the $RM_{dp\%}$ column.

The results show that shareholder value is inversely related to the level of default risk: the higher the insurer's default probability, the lower the shareholder value. Thus, it is optimal for our "sample" insurer to choose a default probability of 0 percent, regardless of the transaction cost of risk management,²⁶ because there will be an overproportional increase in premium income when reducing the probability of default by 1 percent.²⁷ By choosing a safety level of 0 percent instead of 1 percent, premium income increases from €3,960 to €5,240, that is, by 32 percent. This leads to an increase in shareholder value of 42 percent (from $\leq 2,658.58$ to $\leq 3,785.41$) as compared to the shareholder value at the higher default risk of 1 percent. Moreover, for safety levels of 0 or 1 percent, shareholders need only little or even no additional risk management due to the optimal price of insurance for each chosen default probability. For a default-free insurance contract, around 25 percent of the policyholders will be willing to pay more than 2.5 times the expected loss (see Table 3 for the 75 percent percentile of willingness to pay for a default-free insurance contract as compared to the actuarially fair premium of \in 40). For a default risk of 1 percent, 25 percent of the policyholders will still be willing to accept insurance contracts at a price twice as high as the expected claims payment (see Table 3 for the 75 percent percentile of the willingness to pay for an insurance contract with a default probability of 1 percent). Thus, the premium obtained for each insurance contract sold, together with the equity capital endowment, serves as sufficient safety capital.²⁸ We conducted the same analysis for different amounts of initial capital $(E_0 = \in 100 \text{ and } \in 0)$ and find that independent of the initial equity endowment, choosing a nonzero default probability always requires such a substantial amount of costly additional risk management that a default probability of 0 percent maximizes shareholder value for both equity endowments.

The parameters for the demand curves were derived from our experiment. As they are the main driver for our result that a default probability of zero is optimal for an

²⁶A more realistic modeling of the transaction costs would imply to positively relate them to the level of default risk. However, this would further extend the optimality lead of the 0 percent default probability situation.

²⁷There are different risk management measures that an insurer can undertake in order to achieve the promised default level, as for example, reinsurance, alternative risk transfer, or raising equity capital.

²⁸As the aggregate losses are binomially distributed, the arbitrage-free value of any calculated risk management measure, $RM_{dp\%}$, is the minimum value of risk management measures needed to meet the promised default probability dp%.

insurer, we performed a robustness check to test the sensitivity of our results to changes in these parameters. To that end, we constructed demand curves with parameters that were either 2 standard deviations below or above the actual estimate (see Table 5 for the parameters).²⁹ Our results did not change significantly in either of these specifications. To sum up, the results from our model of an insurance company facing an insurance demand curve that is derived from experimental data on individuals' willingness to pay and that is downward sloping in default risk suggest the following: choosing a nonzero default probability leads to such a sizable decrease in the demand for insurance that the optimal strategy for the insurance company is to eliminate all default risk.

DISCUSSION

Given that policyholders have full information about the insurer's safety situation, our results suggest that the insurer should choose a default-free safety level rather than even a small probability of default. As can be seen in Table 6, the overproportional increase in premium income when reducing the default probability outweighs any costs of risk management necessary to achieve a higher solvency level. This result is in line with Rees, Graveller, and Wambach's (1999) theoretical results on solvency regulation, which show that shareholder value is maximized by reducing the default risk to zero if expected utility-maximizing consumers are fully informed of the insurer's insolvency risk. Our result is of higher empirical validity, however, because we extend the Rees, Graveller, and Wambach approach in two major ways: we allow consumers to be heterogeneous with respect to their purchase behavior, and the insurer faces an empirically observed price-default-demand curve. The question arises as to whether our experimental results can be generalized to other insurance purchase contexts. We believe the answer is "yes." Although individuals' absolute willingness to pay may vary between different settings of insurance purchase decisions, the observed general behavior, that is, the relative differences in willingness to pay between different solvency levels, should remain valid, for two reasons. First, our results confirm previous results in the literature on policyholder reactions to default risk (see Wakker, Thaler, and Tversky, 1997; Albrecht and Maurer, 2000; Zimmer, Schade, and Gründl, 2009): individuals either will not accept default risk or they will ask for a greater than expected reduction in insurance premiums. Moreover, this reaction is sensitive to the level of default probability; that is, the higher the default probability, the lower the willingness to pay (see particularly Zimmer, Schade, and Gründl, 2009). Second, we are the first to demonstrate the robustness of those results in an incentive-compatible experiment. Previous experimental research on policyholder reactions to default risk is based on hypothetical insurance purchase decisions. The insurance purchase decisions in our experiment had real-money consequences. Subjects could buy an insurance contract to protect themselves against a real possible loss.

One reason for the resulting extremely high shareholder values of the insurance company and the respective profitability indices (e.g., a shareholder value to initial

²⁹The results of all robustness checks are available from the authors upon request.

equity capital ratio of 946 percent for risk-free contracts), is our assumption of a monopolistic insurance market in which the insurer is free to set insurance prices to maximize shareholder value. It is, therefore, possible for the insurance company to charge for instance a premium for the default-free contract that is more than three times the actuarially fair premium (€131 as compared to €40, Table 6). To account for competition on the insurance market, we also conduct our analysis under a price regulation regime allowing only a certain level of markup over expected losses.³⁰ We find that our result that a default probability of 0 percent maximizes shareholder value holds even when prices are set at a level that just covers expected losses.³¹

CONCLUSION

In this article, we test the hypothesis of probabilistic insurance by eliciting individuals' willingness to pay for theft insurance contracts with default risk in an experimental setting. Our hypothesis that willingness to pay for insurance decreases overproportionally with increasing default risk cannot be rejected. We are the first to show that the effects of probabilistic insurance are not limited to hypothetical (questionnaire) experiments, but that they instead generalize to an economic, incentive-compatible experiment. While most participants in our experiment were generally willing to buy insurance, their willingness to pay for insurance protection decreased significantly when there was a nonzero probability of contract nonperformance. The median willingness to pay decreases from well above the actuarially fair premium in case of a default-free insurance contract to an amount significantly below the fair premium in case of a 3 percent default probability. This drop in willingness to pay underscores how important insurance is to individuals as a means to completely eliminate risk. This finding is particularly remarkable because it is independent of participants' observable personal characteristics such as gender and risk aversion. We therefore provide not only strong evidence in favor of the hypothesis of probabilistic insurance, but also demonstrate that it applies to individuals from different socioeconomic groups. To make a prediction about the impact of default risk on the demand for insurance outside the laboratory, one needs to take into account that the default probability of an insurance contract is unknown in real life. Instead of a decision under risk, individuals are thus making a decision under ambiguity. In the light of findings on ambiguity aversion with insurance decisions (see Hogarth and Kunreuther, 1989; Schade, Kunreuther, and Koellinger, 2012), we expect the effect of an uncertain default probability on insurance demand to be even larger in real life.

Based on this result, this article additionally provides new evidence on the relationship between an insurer's default situation, the price of insurance, and shareholder value. Based on our experimental results, we derive price-demand curves for several default probabilities. These demand curves are implemented in a shareholder value maximization approach to determine the insurer's optimal level of default risk. Our results suggest that the insurer should choose a default probability of

³⁰The results of this analysis are available from the authors upon request.

³¹Note that such "fair" premiums also contain an implicit markup stemming from discounting.

zero. This corner solution is even optimal for the insurer when assuming substantial costs of risk management undertaken to achieve the maximum solvency level.

Our results can be utilized for regulatory purposes. Providing consumers with information about insurers' default situation appears to have great potential for effectively protecting policyholder interests via market discipline. Our results suggest that disclosure requirements need not actually be very onerous for insurers. Insurers can maximize shareholder value by engaging in a risk policy that ensures solvency. Thus, controlling their solvency level will become critical to the success of insurance companies if they are required to disclose their solvency situations as intended, for example, by the U.S. risk-based capital approach and the European Solvency II regulation (see Holzmüller, 2009).³²

Furthermore, our experimentally based results provide empirical evidence that corporate risk management is a rational course of conduct for the financial services sector. Although the limited liability of shareholders of publicly held insurance companies is conducive to the adoption of risk-prone policies, that is, the exact opposite of engaging in risk management, customers' strong negative reaction to default risk self-enforces an almost riskless firm policy. An outside observer might believe that it is the company itself that is risk averse, instead of such an attitude being the consequence of customer pressure. This may explain why so many theoretical contributions aimed at deriving an optimal firm policy assume a risk-averse insurer or financial services firm instead of taking a more straightforward limited liability shareholder value approach as we have done here (see, e.g., Grossman and Zhou, 1996; Kaluszka and Okolewski, 2008).

APPENDIX A: EXPERIMENTAL INSTRUCTIONS

The complete experiment consisted of two parts. This article is based on the first part, but some of the instructions refer to both parts. All instructions referring to coin collection B are irrelevant to this article and should be disregarded. The instructions are translated from German.

Experimental Instructions

Please imagine yourself in the following situation

- You inherited two coin collections, coin collection A and coin collection B, worth €800 each. You will receive a photo of each collection during the experimental session.
- Unfortunately, only one person out of the entire group of subjects participating in our experiment (180–200 persons) will actually receive a real coin collection A and one person will receive a real coin collection B. All other participants will be given a forgery. We would have liked to give all of you a real coin collection, worth €800, but the budget for our experiment is not large enough.

³²See also Harrington (2005) for a discussion of the relevance of market discipline for the financial stability of insurance companies.

- The persons owning a real coin collection will be chosen at random at the end of the experimental study in January 2008. Participants who own a real coin collection will actually receive the value of the coin collection, worth €800, in cash! It is possible that one person will end up with both real coin collections, in which case that person will receive €1,600 in cash. Thus, when making your decisions, keep in mind that you could be the actual owner of coin collection A and/or coin collection B.
- Furthermore, imagine that you keep coin collection A in your own apartment and coin collection B with your parents' apartment.
- Both coin collections are threatened by the risk of theft. The probability that a theft of your coin collection A or your coin collection B will occur is 5 percent for each collection. The risk of theft can be illustrated with a bingo cage. A 5 percent chance that a theft occurs is comparable to the chance of drawing ball #1 out of 20 numbered balls in a bingo cage.
- You can now buy theft insurance for each of the coin collections you have inherited. Each coin collection will be separately insured against a possible theft.
- At this point, we want to clarify that only the owner of the real coin collection will actually pay for the insurance contract.
- Furthermore, during your research into theft insurance contracts, you read an article stating that insurance contracts can be exposed to the risk of default; that is, there is a small probability that the policyholder will not be reimbursed by the insurer in case of a loss.

Part 1—Coin Collection A³³

In the first part of the experiment you have the opportunity to purchase a theft insurance contract against a possible loss of your coin collection A.

The selling procedure for the theft insurance contract is as follows:

- You do not know the price of the theft insurance contract. Before the experiment, the experimenter selected a secret selling price for the theft insurance contract, which he wrote down and sealed in an envelope and then put the envelope on the front desk.
- You are required to state a buying price equal to your maximum willingness to pay for the theft insurance contract. This is the maximum amount of money you are willing to pay for the insurance contract.
- After the experiment, the experimenter will open the envelope containing the secret selling price. If your buying price is equal to or higher than the secret selling price, you can purchase the theft insurance policy at the secret selling price. If your buying price is lower than the secret price, you will not be allowed to buy the theft insurance contract.

³³Part 2 refers to coin collection B and is not reported here.

- Note that the experimenter changes the secret selling price for every experimental session. So even if someone from a previously conducted experiment has told you the price revealed at their experiment, your secret selling price will be different.
- If you are able to purchase an insurance contract and if you are the person owning the real coin collection, then you will be required to pay the selling price, not the price you actually stated.
- In this situation, your best course of action is to state your maximum willingness to pay for the theft insurance contract.
- First, it does not make sense to state a buying price higher than your maximum willingness to pay since you may end up paying this high price.
- Second, it does not make sense to state a price lower than your maximum willingness to pay because if your stated price is lower than the selling price, you will not be permitted to purchase the theft insurance contract, even if you would be willing to pay the secret selling price.
- If you do not want to buy the theft insurance contract, please mark the appropriate box.
- Please do not announce your buying price to the others and do not ask questions that will allow others to guess your buying price.

As a reminder: We are still talking about the theft insurance contract for coin collection A.

- We will ask you to state your willingness to pay for four different insurance contracts.
- All four contracts have the same scope of indemnity, but each contract has a different level of default risk.
- Each contract has a secret selling price. All selling prices were chosen prior to today's experimental session and are each in a separate envelope on the front desk.
- You can purchase only one of the four insurance contracts (as there is only one coin collection A). The relevant contract will be determined at random. Thus, keep in mind that each purchase decision you make could turn out to be the relevant one.

At the end of today's experiment, you will find out whether or not you have purchased an insurance contract.

• At the end of today's experiment, one of the four insurance contracts will be randomly selected. That contract will then be relevant for all participants. A randomly determined participant will draw a card out of a box containing four cards. The cards are numbered from 1 to 4. The number of the drawn card defines the relevant insurance contract.

- The experimenter will then open the envelope and the secret selling price thus revealed will determine whether or not you have purchased an insurance contract.
- At this point, the experimenter will come to your seat and will note on your photo of coin collection A whether or not you have purchased an insurance contract and, if you have purchased one, at what price. Afterward, the experimenter will collect all photos.

Whether you are the person owning the real coin collection will be determined at the end of the experimental study in January 2008.

- An independent person will draw one photo out of all photos of coin collection A. The participant to whom this photo belongs is the owner of the real coin collection A and thus the owner of €800 in cash.
- If this participant has purchased an insurance contract, he or she must pay the respective price to the experimenter.
- A bingo cage with 20 balls will be used to determine whether or not coin collection A will be stolen. The owner of the real coin collection will draw one ball from the bingo cage. If the ball with the number 1 is drawn, theft will occur. If that participant does not have an insurance contract, he or she will lose coin collection A, and thus €800. If a ball with a number between 2 and 20 is drawn, there will be no theft and the participant will keep the €800.
- Whether or not the insurance company will actually pay the claim in case of a loss (if you have purchased an insurance contract) will also be determined by a bingo cage. The number of balls in the bingo cage and which balls will determine whether or not a default has occurred depend on the level of default risk. Again, the owner of the coin collection will draw the balls.

One Example: If the insurance contract has a default probability of 1 percent, there will be 100 balls in the bingo cage. If the ball with the number 1 is drawn, default occurs and the insurance company will not reimburse the value of the stolen coin collection. In this case, the owner of the coin collection will receive nothing. If a ball with a number between 2 and 100 is drawn, no default occurs and the insurance company will pay the owner of the coin collection \in 800.

You now have the opportunity to purchase a theft insurance contract against a possible loss of your coin collection A. An insurance agent offers you different insurance contracts. All these contracts will reimburse the value of the coin collection A, worth \in 800, in case of theft.

Remember, there is a 5 percent probability that your coin collection will be stolen, which, using the bingo cage as an example, means that the chance a theft occurs is comparable to the chance of drawing ball #1 out of 20 numbered balls in the bingo cage.

Each contract has a different level of default risk, that is, the possibility that the insurer will not pay its valid claims in case of a loss. A 1 percent default risk can be interpreted as follows. One out of 100 policyholders who report a loss will not be reimbursed by the insurer. A 1 percent chance that a default occurs is comparable to the chance of drawing ball #1 out of 100 numbered balls in a bingo cage.

We now present you with four different insurance contracts. We ask you to state your maximum willingness to pay for each of the four contracts.

- Please keep in mind that any one of the four contracts could be the relevant one.
- Thus, you should be aware that each of your decisions could be the relevant one and thus constitute your only chance of buying theft insurance.

APPENDIX B: DETERMINING THE NECESSARY RISK MANAGEMENT MEASURES

Assume that the insurer promises a certain default probability, for example, 1 percent. Depending on the offered insurance price, $\pi_{1\%}$, policyholders will pay $Q\pi_{1\%}$ premium income, which leads to a shareholder value of $SHV_{promised_1\%}$. Note that $SHV_{promised_1\%}$ represents the shareholder value for a 1 percent default risk assuming that enough safety capital is on hand to obtain the 1 percent risk level. The actually resulting default probability can deviate from the promised one, however. To obtain the promised level of default risk, the insurer will need to either undertake additional risk management whose arbitrage-free value, $RM_{1\%}$, is the difference between shareholder value based on the default probability before undertaking additional risk management ($SHV_{actual_dp\%}$) and shareholder value at the 1 percent default level ($SHV_{promised_1\%}$):

$$RM_{1\%} = SHV_{actual_dp\%} - SHV_{promised_1\%}.$$
 (A1)

If *c* represents the transaction cost factor of risk management measures, shareholder value for a safety level of 1 percent is described by

$$SHV_{ensured_1\%} = SHV_{promised_1\%} - cRM_{1\%}.$$
 (A2)

If the promised default situation is already the *status quo* or risk management has zero transaction costs (c = 0), then $SHV_{ensured_1\%} = SHV_{promised_1\%}$. Furthermore, if $RM_{1\%} < 0$, that is, the actual shareholder value is lower than the promised one, the desired (lower) safety level can be achieved by extracting equity capital from the company. Assuming that lowering the level of risk management costs less than increasing it, for the sake of simplicity, we set c = 0 for the first case and c > 0 for the latter. Following this procedure, which is shown in Figure B1, the optimal safety level can now be determined by simply comparing shareholder values for different promised, as well as ensured, levels of default risk.

FIGURE B1

Determination of Optimal Safety Level



Note: The figure summarizes the procedure we use to determine the insurer's optimal safety level, taking the 1 percent default probability situation as an example.

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