# Income Concentration and Its Optimal Taxation 

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## Plan of talk

1. Top Incomes in the Long Run
2. Current Situation in Germany
3. Theory of Optimal Top Tax Rates
4. Application to German Income Tax

## Data sources

- Surveys
- Lack of data before 1960
- Rich people not covered


## Data sources

- Income Tax Statistics
- Tabulated income distributions
- Tax evasion
- Definition of income
- Definition of the income-receiving unit


## 1. Evolution over the XXth Century

- 22 investigated countries: Argentina, Australia, Canada, China, Finland, France, Germany, India, Indonesia, Ireland, Italy, Japan, Netherlands, New Zealand, Norway, Portugal, Singapore, Spain, Sweden, Switzerland, UK, US.
- Main reference: Atkinson \& Piketty (2007)


## Share of top 1\% in Prussia



## The great impoverishment of the rich: Share of top 0.1\%



## The rich strike back: Share of top 0.1\% in English-speaking countries



## Explanations

- The great impoverishment of the rich: A capital-income phenomenon
- Hyperinflation, Great Depression, Wars
- Progressive taxation


## Explanations

- The rich strike back: A wage-income phenomenon (?)
- Global markets for superstars
- Shareholder value
- De-unionization
- Lower top marginal tax rates
- Financial development


## 2. Recent developments in Germany

- Historical background from Dell (2007)
- Period 1992-2003 from Bach, Corneo, and Steiner (2009)


## Share of top 0.01\%



- 1992-2003: ITR-SOEP integrated dataset
- Data matching
- Full coverage of taxpayers in the top percentile


## Top personal real market incomes

| Gross market income ${ }^{1)}$, capital gains excluded | 1992 | 1995 | 1998 | 2001 | 2003 | 1995 | 1998 | 2001 | 2003 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1000 Euro at 2000 prices $^{2}{ }^{\text {a }}$ |  |  |  |  | $1992=100$ |  |  |  |
| Mean income | 20.0 | 19.7 | 19.8 | 19.8 | 19.8 | 98.7 | 99.3 | 99.3 | 99.3 |
| Median income | 12.5 | 11.3 | 9.7 | 8.8 | 8.2 | 90.7 | 77.8 | 70.1 | 65.4 |
| Average income |  |  |  |  |  |  |  |  |  |
| Top 10\% | 77.9 | 77.0 | 80.7 | 83.1 | 82.1 | 98.8 | 103.6 | 106.7 | 105.4 |
| Top 1\% | 224.2 | 210.2 | 229.5 | 240.4 | 222.5 | 93.7 | 102.3 | 107.2 | 99.2 |
| Top 0.1\% | 836.0 | 761.5 | 867.4 | 920.4 | 816.5 | 91.1 | 103.7 | 110.1 | 97.7 |
| Top 0.01\% | 3246.6 | 3065.8 | 3614.6 | 3850.9 | 3567.4 | 94.4 | 111.3 | 118.6 | 109.9 |
| Top 0.001\% | 11064.6 | 11721.3 | 14267.5 | 15161.2 | 16223.9 | 105.9 | 128.9 | 137.0 | 146.6 |
| Top 0.0001\% | 31437.4 | 39051.3 | 47230.2 | 48697.1 | 72793.4 | 124.2 | 150.2 | 154.9 | 231.6 |
| Lowest income |  |  |  |  |  |  |  |  |  |
| Top 10\% | 46.8 | 46.9 | 48.7 | 49.6 | 50.8 | 100.1 | 103.9 | 105.8 | 108.4 |
| Top 1\% | 103.9 | 101.5 | 107.4 | 111.4 | 109.0 | 97.7 | 103.4 | 107.3 | 105.0 |
| Top 0.1\% | 340.7 | 312.2 | 337.9 | 352.7 | 316.4 | 91.6 | 99.2 | 103.5 | 92.9 |
| Top 0.01\% | 1397.8 | 1211.5 | 1384.2 | 1478.8 | 1227.2 | 86.7 | 99.0 | 105.8 | 87.8 |
| Top 0.001\% | 5501.6 | 5257.7 | 6175.9 | 6558.0 | 5576.8 | 95.6 | 112.3 | 119.2 | 101.4 |
| Top 0.0001\% | 18360.4 | 19696.6 | 25456.4 | 27164.4 | 25383.8 | 107.3 | 138.6 | 148.0 | 138.3 |
| 1) Income from business activity, wage income, capital income, exclusive public and private pensions; measured at the individual level.- 2 ) Deflated by consumer price index. <br> Source: ITR-SOEP data base. |  |  |  |  |  |  |  |  |  |

## 3. Optimal tax rate for top incomes

- Continuum of households whose mass is normalized to unity
- Households are either single persons or couples; $\mu=$ share of couples
- Households differ according to their productivity $\omega$, which is their private information
- Income of singles taxed according to $T(y)$; a couple with income y pays $2 T$ (y/2)
- Government sets a marginal tax rate $\tau$ for incomes larger than $\bar{y}$
- Utility functions defined on consumption and leisure, rewritten as $u(c, y)$ where $c$ is consumption and $y=\omega /$ is earnings
- Rawlsian planner chooses $\tau$


## Behavior of top earners

Income tax paid by singles with $y \geq \bar{y}$ is $T(\bar{y})+\tau(y-\bar{y})$; couples with $y \geq 2 \bar{y}$ pay $2 T(\bar{y})+\tau(y-2 \bar{y})$.

Write consumption of singles as: $\quad c=y(1-\tau)+R$
where $\quad R=\tau \bar{y}-T(\bar{y})$

Consumption of couples: $\quad c=y(1-\tau)+2 R$
Utility maximization yields earnings supply function $y_{s}(1-\tau, R)$ for singles and $y_{c}(1-\tau, 2 R)$ for couples

## Planner's choice of $\tau$

Implications of a small $d \tau$ for tax revenue:

- Mechanical effect:

$$
M=\left[(1-\mu)\left(y_{m s}-\bar{y}\right)+\mu\left(y_{m c}-2 \bar{y}\right)\right] d \tau
$$

where $y_{m s}$ is mean of incomes above $\bar{y}$ in the income distribution of singles and $y_{m c}$ is the mean of incomes above $2 \bar{y}$ in the income distribution of couples.

- Behavioral effect decomposed into two parts:
(i) Overall uncompensated increase $d \tau$ in the marginal tax rate starting from 0
(ii) Increase in virtual income equal to $d R=\bar{y} d \tau$ for singles and equal to $d 2 R=2 \bar{y} d \tau$ for couples

$$
\begin{aligned}
& B_{s}=-\tau\left(\varepsilon_{S}^{u} y_{m s}-\eta_{s} \bar{y}\right) \frac{d \tau}{1-\tau} \\
& B_{c}=-\tau\left(\varepsilon_{C}^{u} y_{m C}-2 \eta_{c} \bar{y}\right) \frac{d \tau}{1-\tau}
\end{aligned}
$$

where $\varepsilon^{u}$ is the uncompensated labor supply elasticity and $\eta$ captures the income effect as given by the Slutsky equation

From the optimality condition $M+B_{S}+B_{C}=0$ one obtains
Propostion 1: The optimal top marginal tax rate is implicitly given by:

$$
\frac{\tau}{1-\tau}=\frac{(1-\mu)\left(y_{m s}-\bar{y}\right)+\mu\left(y_{m c}-2 \bar{y}\right)}{(1-\mu)\left(\varepsilon_{s}^{u} y_{m s}-\eta_{s} \bar{y}\right)+\mu\left(\varepsilon_{C}^{u} y_{m c}-2 \eta_{c} \bar{y}\right)}
$$

## A simple special case

Assumptions:

- Top earnings are Pareto distributed, i.e. there exists $k \in(0, \bar{y}]$ such that

$$
1-F(y)=\left(\frac{y}{k}\right)^{-\alpha}
$$

where F is the cumulative distributive function and $y \geq k$

- $\quad \varepsilon_{S}^{u}=\varepsilon_{C}^{u}=\varepsilon^{u}$

$$
\eta_{S}=\eta_{C}=\eta
$$

$$
\alpha_{S}=\alpha_{C}=\alpha
$$

Proposition 2: Under the assumptions made, the optimal top marginal tax rate is

$$
\tau=\frac{1}{1+\alpha \varepsilon^{u}-(\alpha-1) \eta}=\frac{1}{1+\varepsilon^{u}+(\alpha-1) \varepsilon^{c}}
$$

## Taxation of consumption

Posit a consumption tax at rate $t$ so that

$$
c(1+t)=y-T(y) .
$$

Proposition 3: In presence of a consumption tax, the optimal top marginal income tax rate is

$$
\tau_{y}=\tau-(1-\tau) t
$$

## 4. Quantification for Germany

Formula:

$$
\tau_{y}=\tau-(1-\tau) t
$$

where

$$
\frac{\tau}{1-\tau}=\frac{(1-\mu)\left(y_{m s}-\bar{y}\right)+\mu\left(y_{m c}-2 \bar{y}\right)}{(1-\mu)\left(\varepsilon_{s}^{u} y_{m s}-\eta_{s} \bar{y}\right)+\mu\left(\varepsilon_{C}^{u} y_{m c}-2 \eta_{c} \bar{y}\right)}
$$

$t=0.19$
$\mu, y_{m s}, y_{m c}$ computed from 2005 ITR $\varepsilon_{S}^{\mu}, \eta_{S}, \varepsilon_{C}^{\mu}, \eta_{C}$ estimated from SOEP

## Ratio of mean wage income above $\bar{y}$ divided by $\bar{y}$



## Ratio of mean wage and selfemployment income above $\bar{y}$ divided by $\bar{y}$



## Ratio of mean wage, selfemployment and business income above $\bar{y}$ divided by $\bar{y}$



## Optimal top marginal income tax rate (\%)

| $\bar{y}$ | Wages | Earnings |
| :---: | :---: | :---: |
| 50,000 | 29.6 | 39.6 |
| 100,000 | 39.5 | 52.2 |
| 300,000 | 53.2 | 62.6 |

